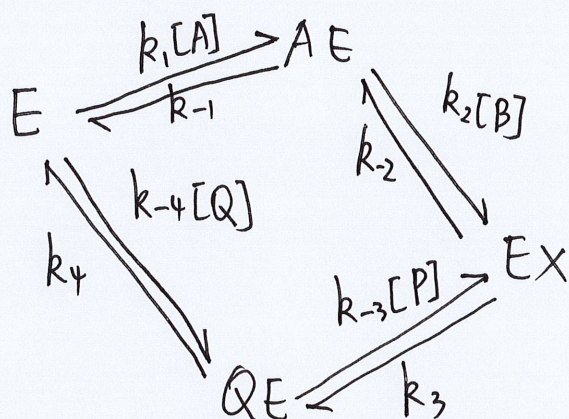
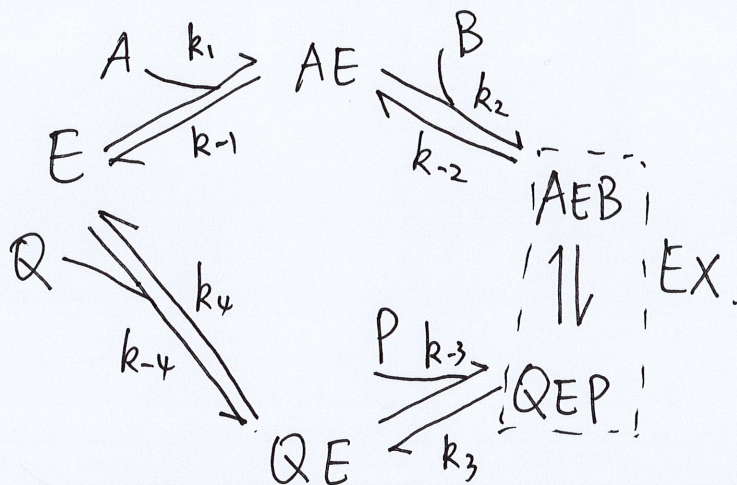
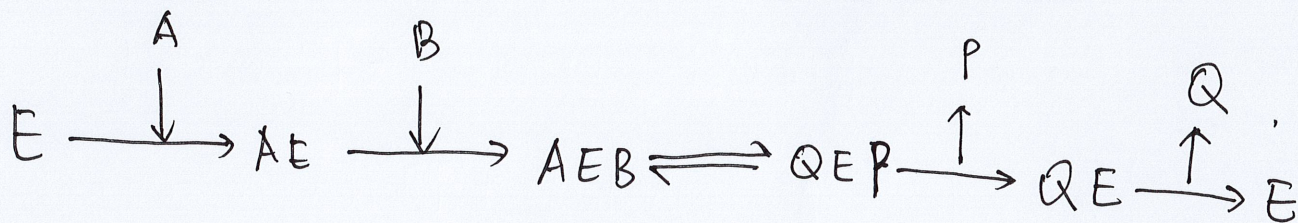
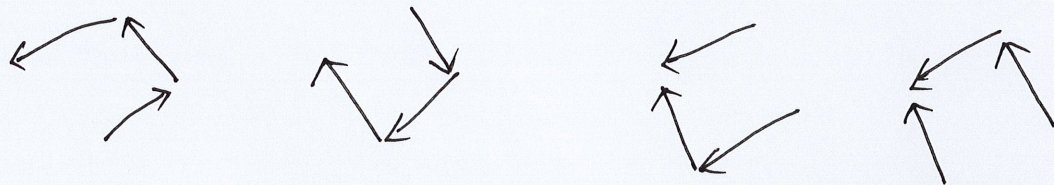


Ordered Bi Bi

2020. 11. 11



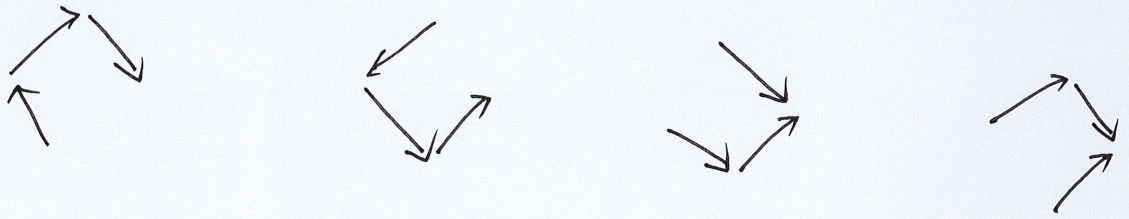
$$\frac{[E]}{[E]_t} = \frac{1}{D} (k_3 k_2 k_1 [P] + k_2 [B] k_3 k_4 + k_1 k_3 k_4 + k_4 k_1 k_2)$$



$$\frac{[AE]}{[E]_t} = \frac{1}{D} (k_3 k_4 k_1 [A] + k_4 [Q] k_3 [P] k_2 + k_1 [A] k_2 k_3 [P] + k_4 k_1 [A] k_2)$$



$$\frac{[EX]}{[E]_t} = \frac{1}{D} \left(k_4 k_1 [A] k_2 [B] + k_1 k_4 [Q] k_3 [P] + k_4 [Q] k_3 [P] k_2 [B] + k_1 [A] k_2 [B] k_3 [P] \right)$$



$$\frac{[QE]}{[E]_t} = \frac{1}{D} \left(k_2 k_1 k_4 [Q] + k_1 [A] k_2 [B] k_3 + k_1 k_4 [Q] k_3 + k_4 [Q] k_2 [B] k_3 \right)$$



$$D = k_1 k_4 (k_2 + k_3) + k_1 k_4 (k_2 + k_3) [A] + k_2 k_3 k_4 [B] + k_1 k_2 k_3 [P] + k_1 k_4 (k_2 + k_3) [Q] + k_1 k_2 (k_3 + k_4) [A] [B] + k_3 k_4 (k_1 + k_2) [P] [Q] + k_1 k_2 k_3 [A] [P] + k_2 k_3 k_4 [B] [Q] + k_2 k_3 k_4 [B] [P] [Q] + k_1 k_2 k_3 [A] [B] [P]$$

$$V = \frac{d[P]}{dt} = k_3 [EX] - k_3 [P] [QE]$$

$$= \frac{k_3 [E]_t}{D} \left(k_4 k_1 k_2 [A] [B] + k_1 k_3 k_4 [P] [Q] + k_2 k_3 k_4 [B] [P] [Q] + k_1 k_2 k_3 [A] [B] [P] \right) - \frac{k_3 [P] [E]_t}{D} \left(k_1 k_2 k_4 [Q] + k_1 k_2 k_3 [A] [B] + k_1 k_3 k_4 [Q] + k_2 k_3 k_4 [B] [Q] \right)$$

$$= \frac{[E]_t}{D} \left(k_1 k_2 k_3 k_4 [A] [B] - k_1 k_2 k_3 k_4 [P] [Q] \right)$$

当 $[P] = [Q] = 0$ 时,

$$\begin{aligned} V &= \frac{k_1 k_2 k_3 k_4 [E]_t [A][B]}{k_{-1} k_4 (k_{-2} + k_3) + k_1 k_4 (k_{-2} + k_3) [A] + k_2 k_3 k_4 [B] + k_1 k_2 (k_3 + k_4) [A][B]} \\ &= \frac{\frac{k_3 k_4}{k_3 + k_4} [E]_t [A][B]}{\frac{k_{-1} k_4 (k_{-2} + k_3)}{k_1 k_2 (k_3 + k_4)} + \frac{k_4 (k_{-2} + k_3)}{k_2 (k_3 + k_4)} [A] + \frac{k_3 k_4}{k_1 (k_3 + k_4)} [B] + [A][B]} \\ &= \frac{V_{\max} [A][B]}{K_s^A K_m^B + K_m^B [A] + K_m^A [B] + [A][B]} \end{aligned}$$

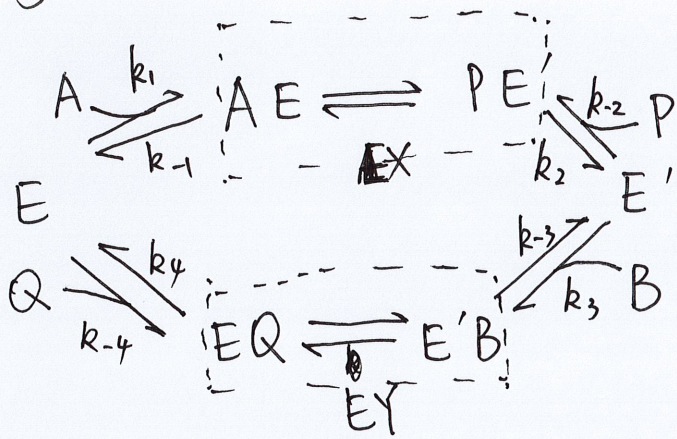
其中

$$V_{\max} = \frac{k_3 k_4}{k_3 + k_4} [E]_t$$

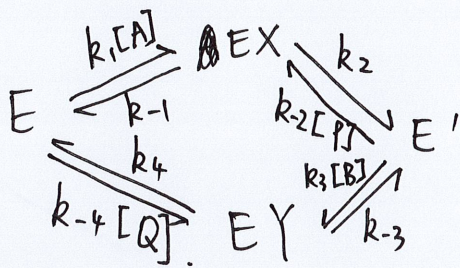
$$K_s^A = \frac{k_{-1}}{k_1}, \quad K_m^A = \frac{k_3 k_4}{k_1 (k_3 + k_4)}, \quad K_m^B = \frac{k_4 (k_{-2} + k_3)}{k_2 (k_3 + k_4)}$$

Ping-Pong bi-bi Rate equation.

2020.11.11. ①

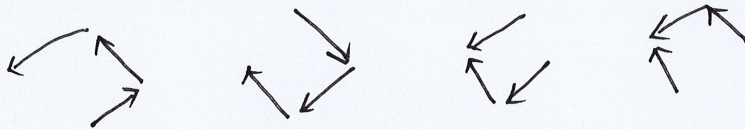


↓

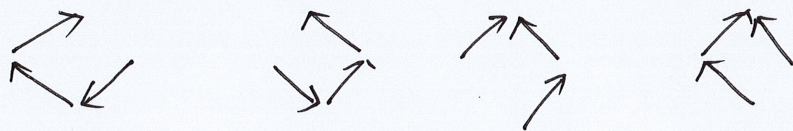


根据 King-Altman Method.

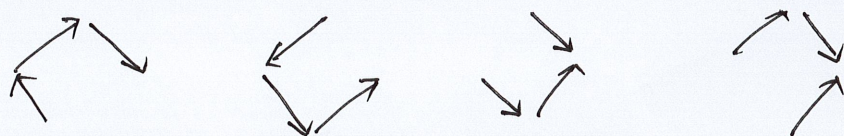
$$\frac{[E]}{[E]_t} = \frac{1}{D} (k_{-1} k_{-2} [P] k_{-3} + k_4 k_3 [B] k_2 + k_{-1} k_4 k_3 [B] + k_4 k_{-1} k_{-2} [P])$$



$$\frac{[EX]}{[E]_t} = \frac{1}{D} (k_1 [A] k_4 k_3 [B] + k_{-2} [P] k_{-3} k_{-4} [Q] + k_1 [A] k_{-2} [P] k_{-3} + k_{-2} [P] k_1 [A] k_4)$$



$$\frac{[E']}{[E]_t} = \frac{1}{D} (k_4 k_1 [A] k_2 + k_{-1} k_{-4} [Q] k_{-3} + k_2 k_{-3} k_4 [Q] + k_1 [A] k_2 k_{-3})$$



$$\frac{[EY]}{[E]_t} = \frac{1}{D} (k_{-2} [P] k_{-1} k_{-4} [Q] + k_1 [A] k_2 k_3 [B] + k_{-4} [Q] k_3 [B] k_2 + k_{-1} k_{-4} [Q] k_3 [B])$$



$$\begin{aligned}
 D &= k_{-1}k_{-2}(k_{-3}+k_4)[P] + k_{-3}k_{-4}(k_{-1}+k_2)[Q] \\
 &+ k_1k_2(k_{-3}+k_4)[A] + k_3k_4(k_{-1}+k_2)[B] \\
 &+ k_1k_3(k_2+k_4)[A][B] + k_2k_{-4}(k_{-1}+k_{-3})[P][Q] \\
 &+ k_1k_{-2}(k_{-3}+k_4)[A][P] + k_3k_{-4}(k_{-1}+k_2)[B][Q].
 \end{aligned}$$

$$v = \frac{d[P]}{dt} = k_2[E] - k_{-2}[E'] [P].$$

$$\begin{aligned}
 &= \frac{k_2[E]_t}{D} \left(k_1k_3k_4[A][B] + k_{-2}k_{-3}k_{-4}[P][Q] \right. \\
 &\quad \left. + k_1k_{-2}(k_{-3}+k_4)[A][P] \right)
 \end{aligned}$$

$$- \frac{k_{-2}[E]_t[P]}{D} \left(k_1k_2(k_{-3}+k_4)[A] + k_3k_{-4}(k_{-1}+k_2)[Q] \right)$$

$$= \frac{[E]_t}{D} \cdot k_1k_2k_3k_4[A][B].$$

由于是初速度, 可以将 $[P]=[Q]=0$ 代入 D 的表达式 即得

$$v = \frac{k_1k_2k_3k_4[E]_t[A][B]}{k_1k_2(k_{-3}+k_4)[A] + k_3k_4(k_{-1}+k_2)[B] + k_1k_3(k_2+k_4)[A][B]}$$

~~$$\begin{aligned}
 v_{\max} &= \frac{k_2[E]_t}{K_M} = \frac{k_2(k_{-3}+k_4)}{k_1}, & K_M &= \frac{k_2(k_{-3}+k_4)}{k_1} \\
 &= \frac{k_2k_4}{k_2+k_4} [E]_t [A][B] \\
 &= \frac{k_2(k_{-3}+k_4)}{k_3(k_2+k_4)} [A] + \frac{k_4(k_{-1}+k_2)}{k_1(k_2+k_4)} [B] + [A][B].
 \end{aligned}$$~~